

TRENDS IN INTERNATIONAL MATHEMATICS AND SCIENCE STUDY

TIMSS

TIMSS 2011 International Results in Mathematics

Ina V.S. Mullis, Michael O. Martin, Pierre Foy,
and Alka Arora



TIMSS & PIRLS
International Study Center
Lynch School of Education, Boston College

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